DKPI Indian Summer School - lecture III



Josef Pradler Sept 21-24 2015





Summary from lecture 2

- Established the basic properties of DM (stability, neutrality, cold, collision- and dissipationless, "size")
- The Boltzmann equation governs the time evolution of the distribution function. It is
 put to great use for the calculation of the relic abundance of dark matter
 (classification of dark matter particles follows by inquiring their by their abundance
 in the early universe)
- WIMPS regulate their abundance through the equation

$$\frac{dn_{\chi}}{dt} + 3\frac{\dot{a}}{a}n_{\chi} = -\sum_{X} \langle \sigma_{\chi\bar{\chi}\to X\bar{X}}v \rangle \left[n_{\chi}^2 - (n_{\chi}^{\text{eq}})^2\right]$$

WIMPs are the primary target for direct detection experiments, that are entering a
decisive phase until they touch the irreducible "neutrino floor".

Plan of the lectures

Lecture 1

- Fundamentals of standard cosmology
- Gravitational evidence for Dark Matter

Lecture 2

- Basic properties of Dark Matter
- The Boltzmann equation and its applications for the early Universe
- WIMP Dark Matter
- Direct Detection of WIMPs

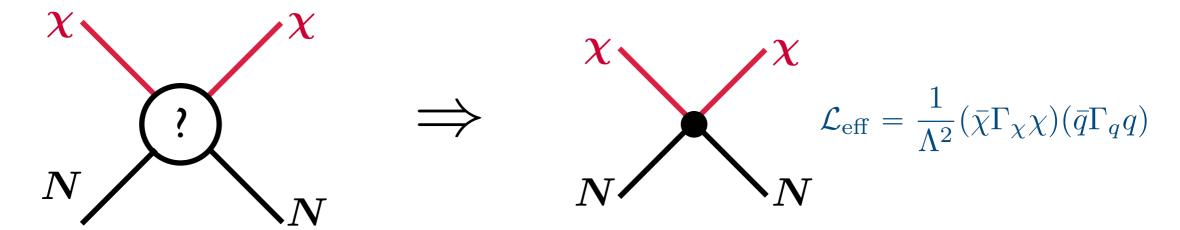
Lecture 3

- Effective operator approach
- Mediators force carriers between the hidden and observable sector
- An alternative to the WIMP miracle
- The origin of chemistry Big Bang Nucleosynthesis

Effective Operators in direct detection

see, in particular, Fan, Reece, Wang (2010) Fitzpatrick et al. (2013)

• Effective operator approach between DM χ and nucleons N often holds as $|q_{\rm max}| \sim O(100\,{
m MeV})$



For example, fermionic DM

Non-relativistic limit (on tree level):

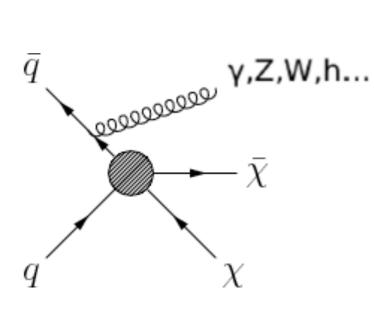
 $S \times S$ or $V \times V$ coherent, spin-independent scattering $A \times A$ or $T \times T$ spin-dependent, coupling to the unpaired nucleon other combinations are suppressed by $v^2, \mathbf{q}^2/m_N^2 \sim 10^{-6}$

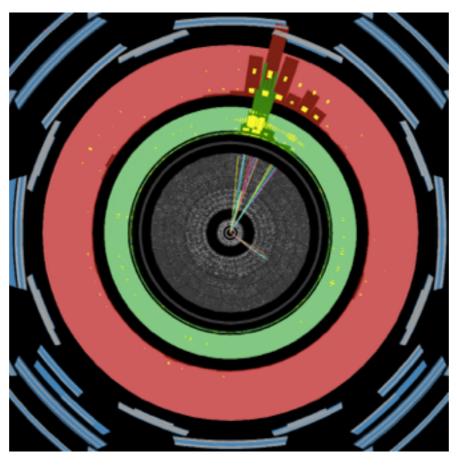
WIMPs 5

Dark Matter at the LHC

 Effective theory in which only the DM and SM fields appear (=contact) provide the simplest parameterization of new physics

=> mono-jet/photon/W/Z + missing momentum





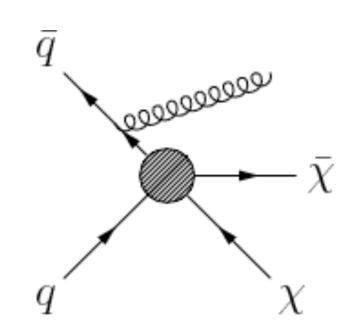
Name	Operator	Coefficient
D1	$ar{\chi}\chiar{q}q$	m_q/M_st^3
D2	$ar{\chi}\gamma^5\chiar{q}q$	im_q/M_*^3
D3	$ar{\chi}\chiar{q}\gamma^5q$	im_q/M_*^3
D4	$ar{\chi}\gamma^5\chiar{q}\gamma^5q$	m_q/M_*^3
D5	$ar{\chi}\gamma^{\mu}\chiar{q}\gamma_{\mu}q$	$1/M_*^2$
D6	$ar{\chi}\gamma^{\mu}\gamma^5\chiar{q}\gamma_{\mu}q$	$1/M_*^2$
D7	$ar{\chi}\gamma^{\mu}\chiar{q}\gamma_{\mu}\gamma^5q$	$1/M_*^2$
D8	$\bar{\chi}\gamma^{\mu}\gamma^5\chi\bar{q}\gamma_{\mu}\gamma^5q$	$1/M_*^2$
D9	$ar{\chi}\sigma^{\mu u}\chiar{q}\sigma_{\mu u}q$	$1/M_*^2$
D10	$ar{\chi}\sigma_{\mu u}\gamma^5\chiar{q}\sigma_{lphaeta}q$	i/M_*^2
D11	$ar{\chi}\chi G_{\mu u}G^{\mu u}$	$lpha_s/4M_*^3$
D12	$ar{\chi}\gamma^5\chi G_{\mu u}G^{\mu u}$	$ilpha_s/4M_*^3$
D13	$ar{\chi}\chi G_{\mu u} ilde{G}^{\mu u}$	$ilpha_s/4M_*^3$
D14	$ar{\chi} \gamma^5 \chi G_{\mu u} ilde{G}^{\mu u}$	$\alpha_s/4M_*^3$

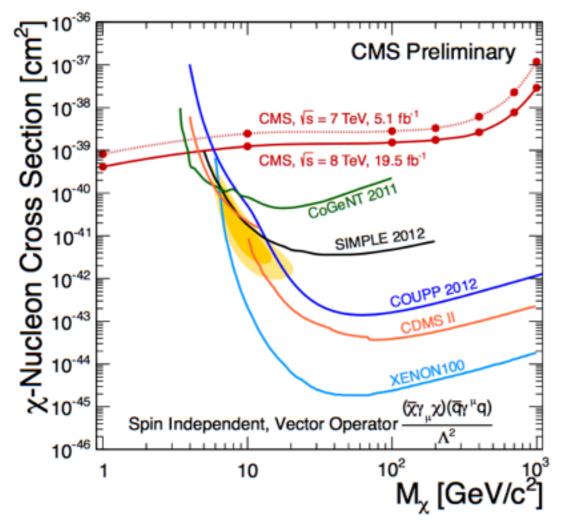
e.g. Goodman et al 2010

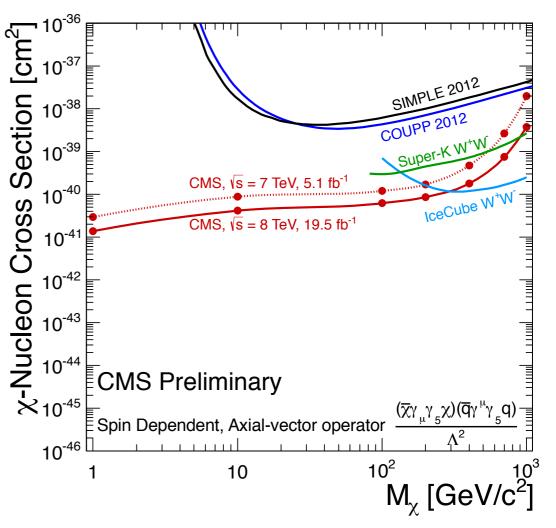
DM at the LHC

LHC does exquisitely well for

- low WIMP masses $m_\chi \lesssim 10\,{
 m GeV}$
- operators that are velocity suppressed in direct detection



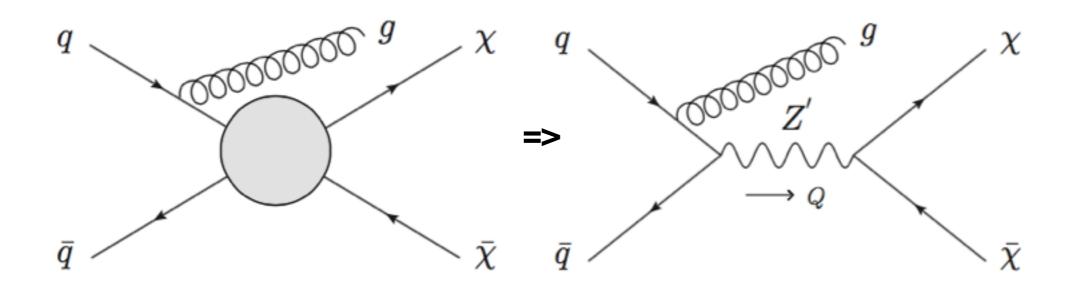




(same data-set as at EPS 2015)

DM at the LHC

Effective field theory approach breaks down, once $q^2 \simeq m_{\rm mediator}^2$



$$\frac{g_q g_\chi}{Q^2 - m_{\rm med}^2} \approx -\frac{g_q g_\chi}{m_{\rm med}^2} \qquad \Longrightarrow \qquad \frac{g_q g_\chi}{Q^2 - m_{\rm med}^2} \approx \frac{g_q g_\chi}{Q^2}$$

$$\Lambda \equiv rac{m_{
m med}}{\sqrt{g_q\,g_\chi}}$$
 contact interaction

 $\langle Q^2 \rangle^{1/2} \gtrsim 500 \, {
m GeV}$ @ 8TeV LHC

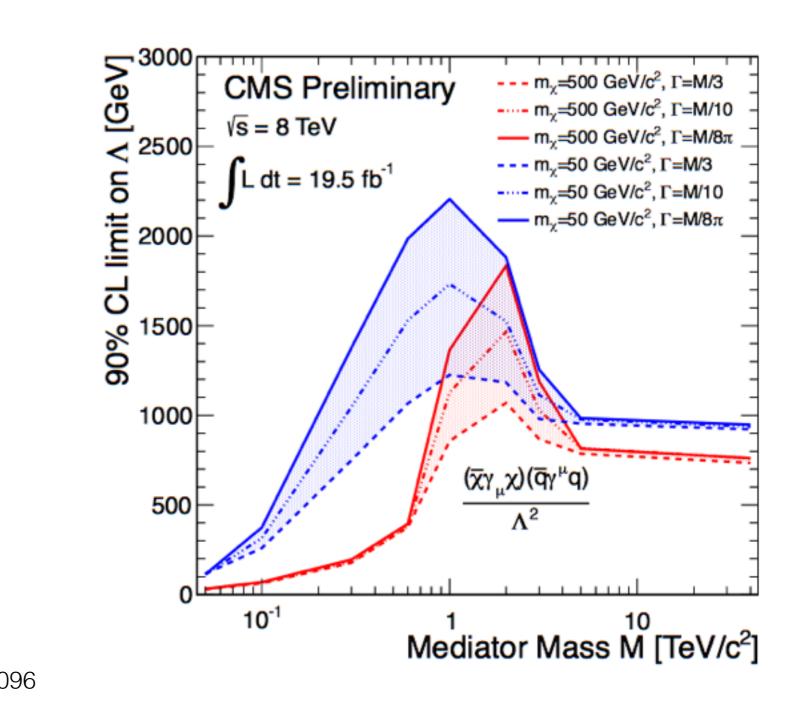
Beyond effective operators

=> results can be cast as a limit on the contact interaction scale Λ

LHC limits are stringent for contact operators, but can go away completely for light mediators!

=> accessible UV content can be caught in "simplified models" with content **SM + DM + mediator**

e.g. arXiv:1507.0096



Mediators

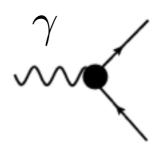
What are the force carriers/mediators?



Photon:

milli-charged DM; neutral DM interacting via EM form factors

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... Kouvaris (2013);
Ho, Scherrer (2013);
Weiner, Yavin (2013)...
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Higgs boson:

Inert Higgs, Higgs portal models, SUSY

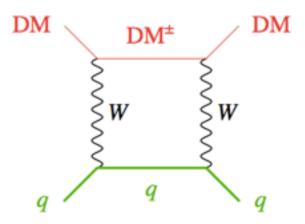
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Deshpande, Ma (1978);
Silveira, Zee (1985);
McDonald (1993);
Burgess, Pospelov, ter Veldhuis (2000)
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EW-bosons:

DM in electroweak multiplets

Cirelli, Fornengo, Strumia (2007)



New physics mediators

squarks, SUSY gauginos, dark photons... (whatever you can think of)

The role of the Higgs - I

Neutralinos of SUSY stabilized by R-parity as DM

Bino, Wino
$$\mathcal{M}_{\chi} = \begin{pmatrix} M_1 & 0 & -m_Z c_\beta s_W & m_Z s_\beta s_W \\ 0 & M_2 & m_Z c_\beta c_W & -m_Z s_\beta c_W \\ -m_Z c_\beta s_W & m_Z c_\beta c_W & 0 & -\mu \\ m_Z s_\beta s_W & -m_Z s_\beta c_W & -\mu & 0 \end{pmatrix}$$
 Higgsinos

Expectation we had: $M_{1,2}, \mu \sim \mathcal{O}(100\,\mathrm{GeV})$ => substantial mixing

Non-observation of SUSY at LHC pushes mass scales => diagonal dominance of

$$\chi$$
 Majorana => $(\bar{\chi}\gamma^{\mu}\chi)(n\gamma_{\mu}n)$ => spin-spin or scalar exchange at LO => Higgs exchange contributes to SI

Original expectations

The "weakly" interacting 100 GeV WIMPs are long excluded

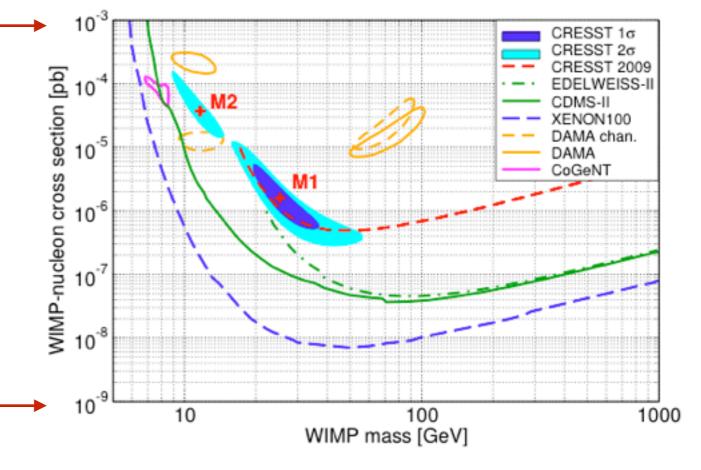


Z-mediated cross section

$$\sigma_n \sim 10^{-3} \, \mathrm{pb}$$

Higgs-mediated interactions are being probed right now!

$$\sigma_n \sim 10^{-(9-10)} \, \text{pb}$$



NB: direct detection may never completely exclude neutralino:

pure neutralino (wino, bino, higgsino) has suppressed higgs couplings $h^{\dagger}\widetilde{h}\widetilde{w}$ $h^{\dagger}\widetilde{h}\widetilde{b}$ pure wino/bino does not couple to Z cancelations in couplings to Z and Higgs

The role of the Higgs - II

"Higgs Portal"

$$\mathcal{L}_{\rm int} = -\lambda S^2(H^{\dagger}H)$$

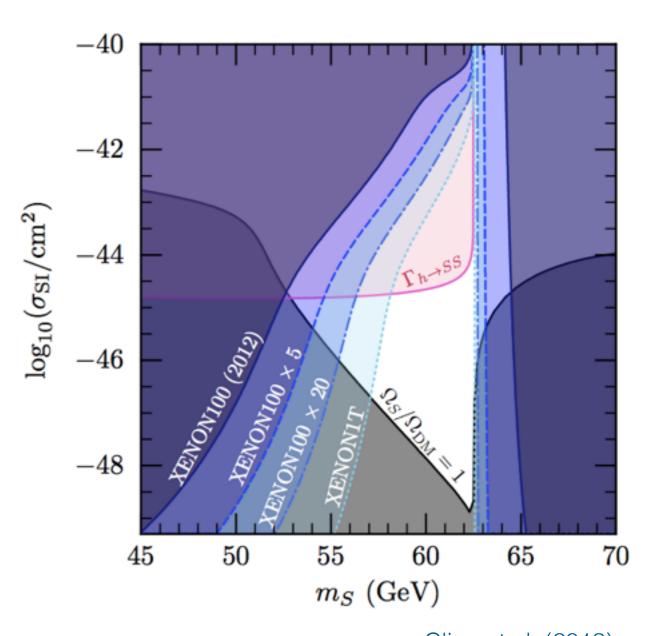
=> relic abundance via annihilation through H

=> direct detection via $\langle n|m_q\bar{q}q|n\rangle$ H-nucleon coupling

• LHC results slain DM models with $m_{\rm DM} \lesssim 60\,{\rm GeV}$

Higgs decays invisibly into DM

=> light-DM models run out of SM mediators



e.g. Cline et al. (2013)

Light Dark Matter

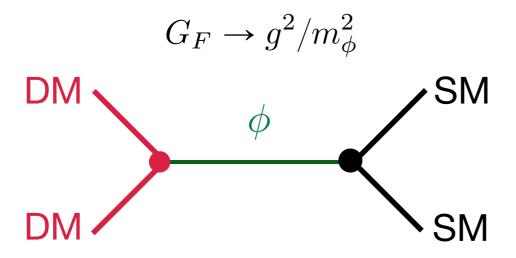
Relic Abundance issues

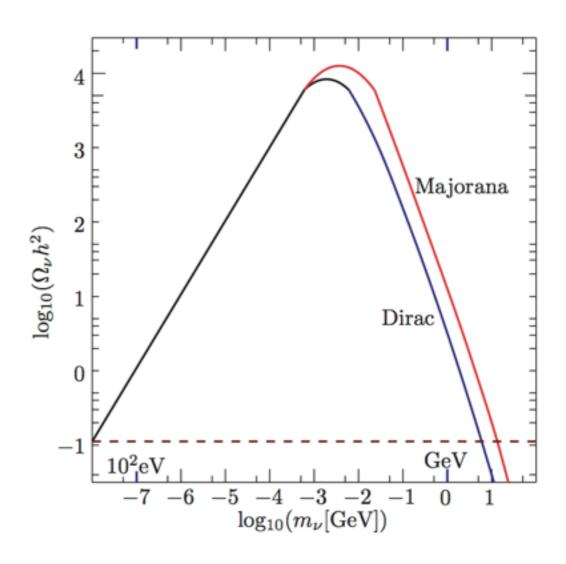
Lee-Weinberg bound:

Annihilation of a heavy neutrino through SM mediators excludes masses below ~ few GeV

$$\langle \sigma v \rangle \sim G_F^2 m_\nu^2 / 2\pi$$

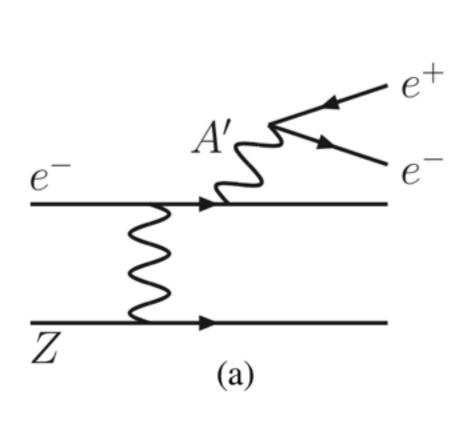
A way out are new, light mediators

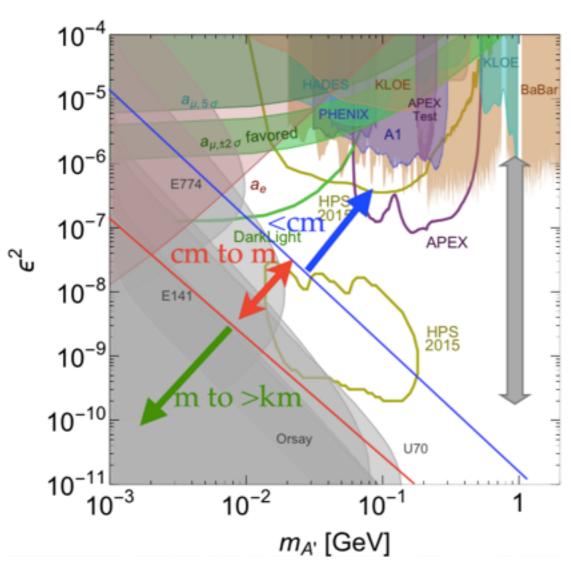




Light Dark Matter - light mediators

The search for light mediators has become a field of its own "intensity frontier"

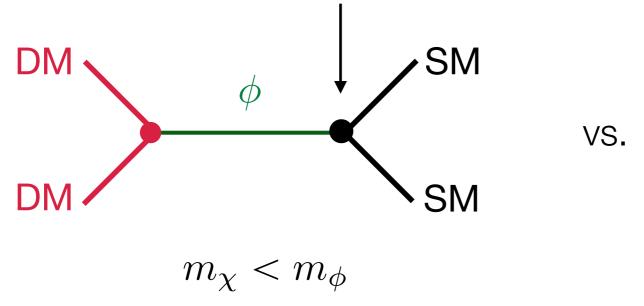


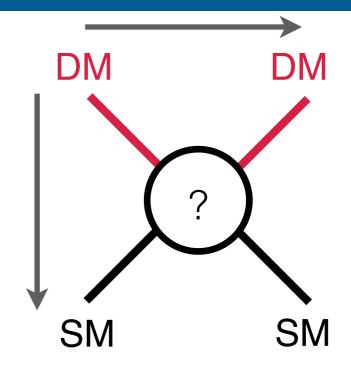


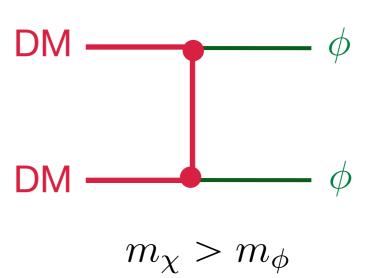
Light mediators, "force carriers of the hidden sector", make a frequent occurrence. They are a minimal extension, make models "work", and they open up new phenomenological signatures.

Do light mediators imply an enhanced direct detection rate?

here a minimum coupling to SM required for efficient annihilation





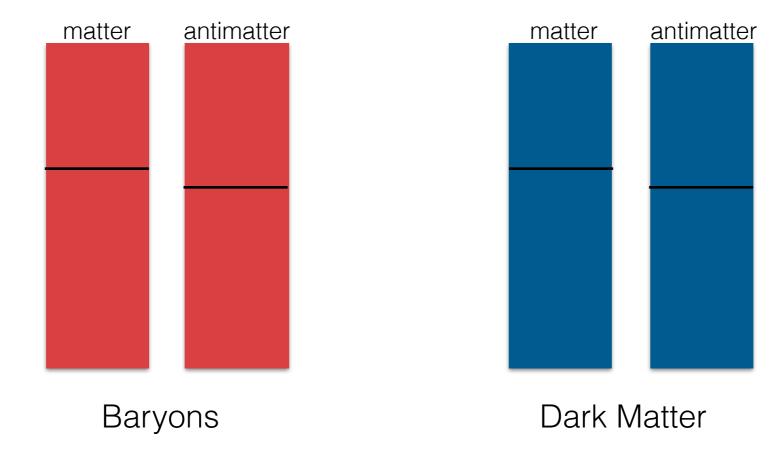


The right situation can completely elude direct detection, because couplings to SM can be small, "cascade annihilation". So, it depends...

An alternative to the WIMP miracle

$$\Omega_{dm} \simeq 5\Omega_b$$
 — Why?

Maybe because dark matter carries a chemical potential (i.e. a matter-antimatter asymmetry)

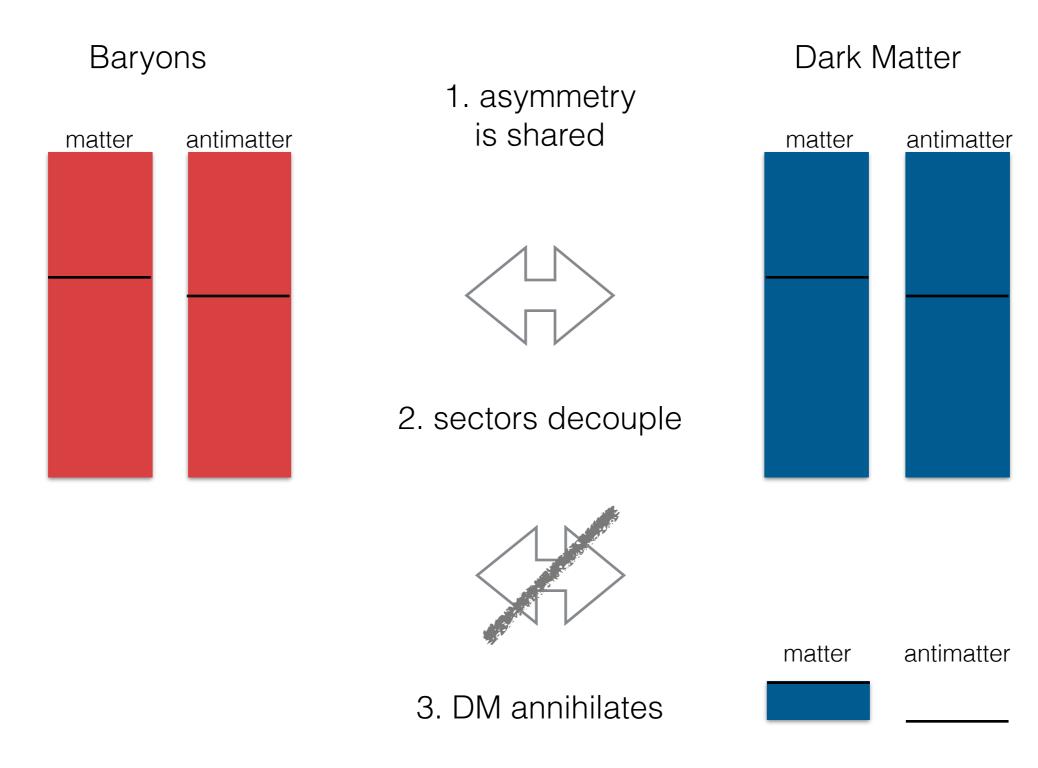


An alternative to the WIMP miracle



Without a chemical potential of baryons, we would be living in a Universe with $n_b/n_\gamma=10^{-18}$ and not $n_b/n_\gamma=10^{-10}$

An alternative to the WIMP miracle



=> abundance is set by the chemical potential

An alternative to the WIMP miracle - asymmetric DM

$$n_{\chi} - n_{\bar{\chi}} \sim n_B - n_{\bar{B}}$$

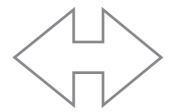
Use sphalerons, or higher dimensional operators

$$\mathcal{O}_{B-L} = u^c d^c d^c$$
, $q\ell d^c$, $\ell\ell e^c$, $\ell\ell H_u$

$$\mathcal{O}_D = X^n$$

$$W = \frac{\mathcal{O}_D \mathcal{O}_{B-L}}{M^{m+n-3}}$$

1. asymmetry is shared



Dark Matter



An alternative to the WIMP miracle - asymmetric DM



1. asymmetry is shared

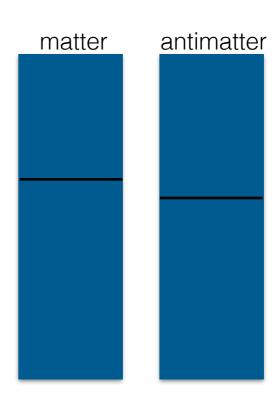


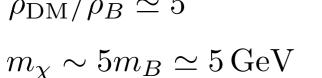
2. sectors decouple



3. DM annihilates









antimatter

 $\rho_{\rm DM}/\rho_B \simeq 5$

An alternative to the WIMP miracle - asymmetric DM

Relic density determined by chemical potential.

Annihilation must be efficient enough to remove the symmetric abundance:

EW scale mediators don't work, required couplings are excluded by LHC.

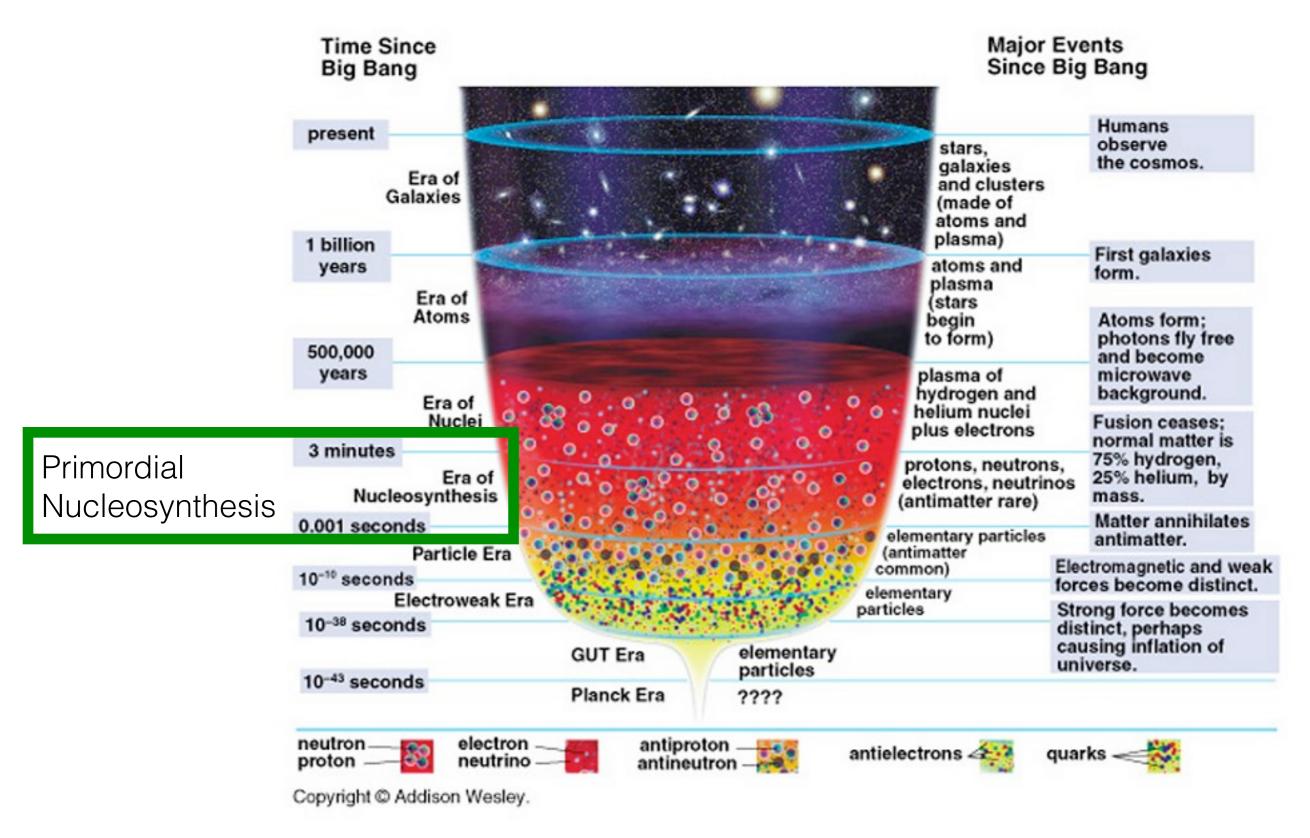
$$\sigma_{ann}v = \frac{g_d^2 g_f^2 m_X^2}{\pi m_M^4} \simeq 10^{-26} \text{ cm}^3/\text{s} \left(\frac{g_d g_f}{0.25}\right)^2 \left(\frac{10 \text{GeV}}{m_X}\right)^2 \left(\frac{200 \text{ GeV}}{m_M}\right)^4$$

Again, relic abundance typically relies on new, light mediators that enhance annihilation cross section.

Note: Indirect detection prospects / astro-constraints depend on the residual abundance of anti-DM after freeze out! The symmetric component does not annihilate.

Detection prospects are built on the interaction that annihilates the symmetric component (model dependent.)

The origin of chemistry



The origin of chemistry

hydrog 1 H	'9																		helium 2 He 4.0026
lithiu 3	m D	eryllium 4												boron 5	carbon 6	nitrogen 7	oxygen 8	fluorin 9	neon
ľ	:	n -														l Ki l		l	NI-
		Be ∣												В	C	N	0	F	Ne
6.94		9.0122												10.811	12.011	14.007	15.999	18,998 chlorine	20.180
11		ignesium 12												aluminium 13	silicon 14	phosphorus 15	sulfur 16	17	argon 18
Na	a N	Иg												ΑI	Si	P	S	CI	Ar
22.99		24.305		canadium	titanium		a bramium	**********	inne	achait	nieka!	******	nin e	26.982	28.086	30.974	32.065	35.453 bromine	39.948
potass 19		calcium 20		scandium 21	titanium 22	vanadium 23	chromium 24	manganese 25	26	cobalt 27	nickel 28	copper 29	zinc 30	gallium 31	germanium 32	arsenic 33	selenium 34	35	krypton 36
K		Ca		Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
39.09		40.078		44.956	47.867	50.942	51.996	54.938	55.845	58.933	58.693	63.546	65.39	69.723	72.61	74.922	78.96	79.904	83.80
rubidii 37		trontium 38		yttrium 39	zirconium 40	niobium 41	molybdenum 42	technetium 43	ruthenium 44	rhodium 45	palladium 46	silver 47	cadmium 48	indium 49	tin 50	antimony 51	tellurium 52	iodine 53	xenon 54
RI		Sr		Ÿ	Žr	Nb	Мо	Tc	Ru	Rh	Pd	Ag	Cd	ĺ'n	Sn	Sb	Te	Ĩ	Хe
85.46		87.62		88.906	91.224	92.906	95.94	[98]	101.07	102.91	106.42	107.87	112,41	114.82	118.71	121.76	127.60	126.90	131.29
caesii	ım t	barium		lutetium	hafnium	tantalum	tungsten	rhenium	osmium	iridium	platinum	gold	mercury	thallium	lead	bismuth	polonium	astatine	radon
55		56	57-70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86
C:		Ba∣	*	Lu	Hf	Ta	W	Re	Os	lr	Pt	Au	Hg	ΤI	Pb	Bi	Po	At	Rn
132.9		137.33		174.97	178.49 rutherfordium	180.95 dubnium	183.84	186.21	190.23	192.22	195.08	196.97	200.59	204.38	207.2	208.98	[209]	[210]	[222]
francii 87		radium 88	89-102	103	104	105	seaborgium 106	bohrium 107	hassium 108	meitnerium 109	ununnilium 110	unununium 111	ununbium 112		ununquadium 114				
Fi		Ra	* *	Ľr	Rf	Db	Sg	Bh	Hs	Mt		Uuu			Uuq				
[223		[226]		[262]	[261]	[262]	[266]	[264]	[269]	[268]	[271]	[272]	[277]		[289]				

*Lanthanide series

* * Actinide series

	lanthanum 57	cerium 58	praseodymium 59	neodymium 60	promethium 61	samarium 62	europium 63	gadolinium 64	terbium 65	dysprosium 66	holmium 67	erbium 68	thulium 69	ytterbium 70
1	La	Се	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Но	Er	Tm	Yb
	138.91	140.12	140.91	144.24	[145]	150.36	151.96	157.25	158.93	162.50	164.93	167.26	168.93	173.04
	actinium	thorium	protactinium	uranium	neptunium	plutonium	americium	curium	berkelium	californium	einsteinium	fermium	mendelevium	nobelium
	89	90	91	92	93	94	95	96	97	98	99	100	101	102
	Ac	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No
	[227]	232.04	231.04	238.03	[237]	[244]	[243]	[247]	[247]	[251]	[252]	[257]	[258]	[259]

Big Bang Nucleosynthesis (BBN) - A pillar of modern cosmology

- recent progress primarily clarifies state of the Universe at z = few (Galaxy surveys, SN,...) and exposes relevant physics at recombination z = 1000
- light element formation happens at $\,z=10^9\,$; direct window into the early Universe at t=1sec
- qualitative agreement between $z = 0 \div 10^3$ and $z = 10^9$ tells us that early Universe was governed by the same physical laws and contained similar particle content
 - => invaluable piece that helps to establish the standard cosmological model
- BBN can react sensitively on departures from General Relativity and the Standard Model of particle physics => a toolbox to test new physics

Basic assumptions for "Standard BBN"

Universe is flat, spatially homogeneous and isotropic and dominated by radiation
 Seneral Relativity:

$$H \equiv \frac{\dot{a}}{a} = \sqrt{8\pi G_N \rho/3} \simeq \frac{1}{2t}$$

• Universe was "hot" enough $T|_{\mathrm{init}}\gg \Delta m_{np}=1.293~\mathrm{MeV}$

$$(n_n \simeq n_p)|_{T \gg \Delta m_{np}} = \frac{1}{2} n_b$$

Particle content & their interactions given by the SM

$$\frac{n_b}{s}(t_{\rm BBN}) = \frac{n_b}{s}(t_{\rm CMB}).$$
 => "parameter free theory"

Excellent approximations

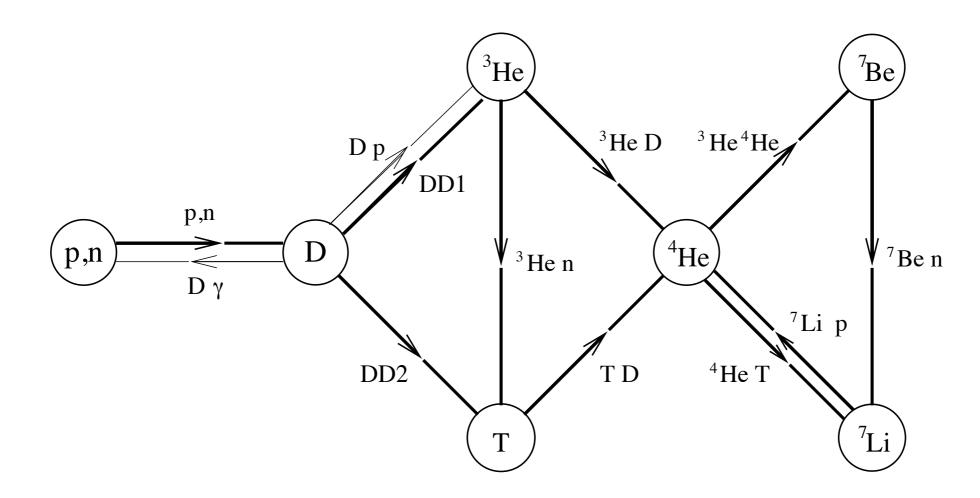
tight kinetic coupling of nucleons/nuclei to the radiation field
 nucleons/nuclei are approximately thermally distributed

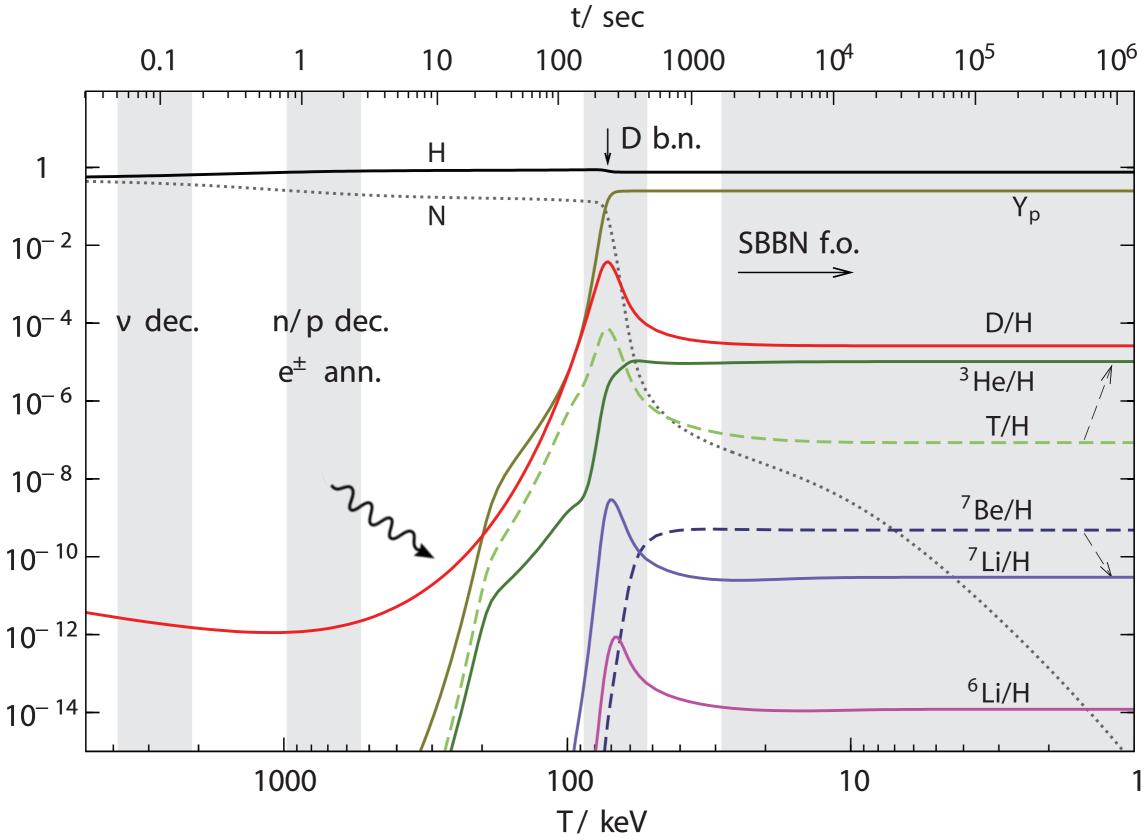
$$\Gamma(E,T) = n \, v \times \sigma \qquad \rightarrow \qquad \Gamma(T) = n \, \langle \sigma v \rangle$$

=> their abundances are found by solving the coupled set of integrated Boltzmann equations

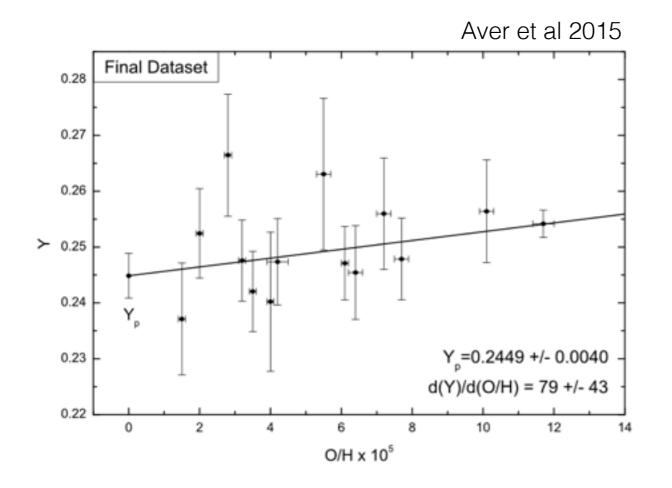
$$\frac{dn_3}{dt} + 3Hn_3 = n_1 n_2 \langle \sigma_{1+2 \to 3+X} v \rangle - n_3 \Gamma_{\text{des},3}$$

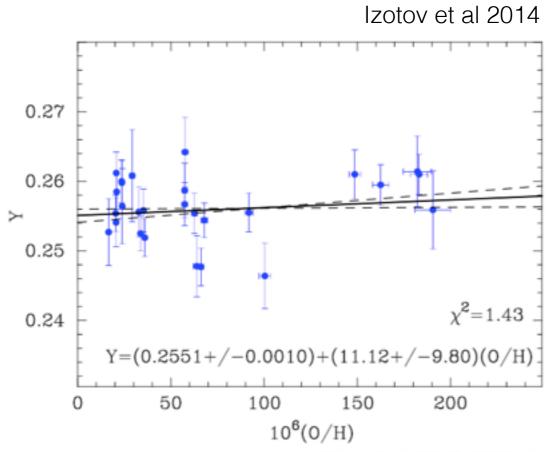
Nuclear reaction network





Light element observations Helium mass fraction $Y_p \simeq 25\%$

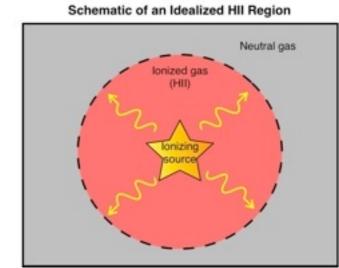




Helium gets illuminated in HII (ionized hydrogen) regions

=> emission lines

now claim few %-level accuracy (systematics limited)

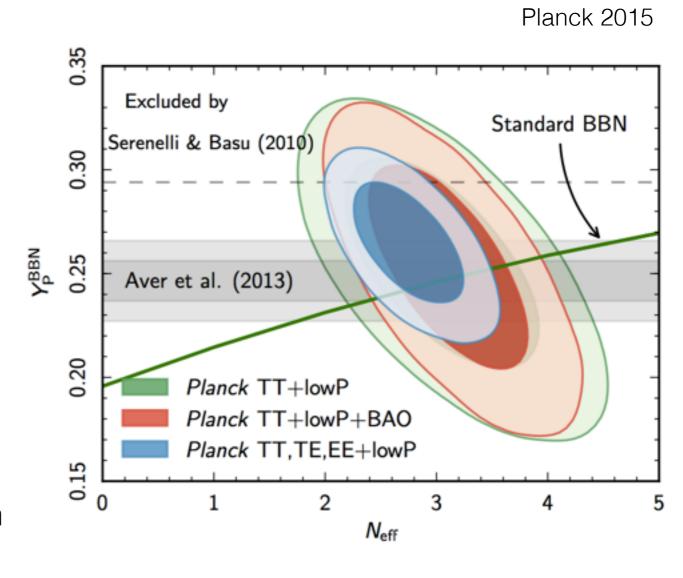


Light element observations Helium @ z=1000

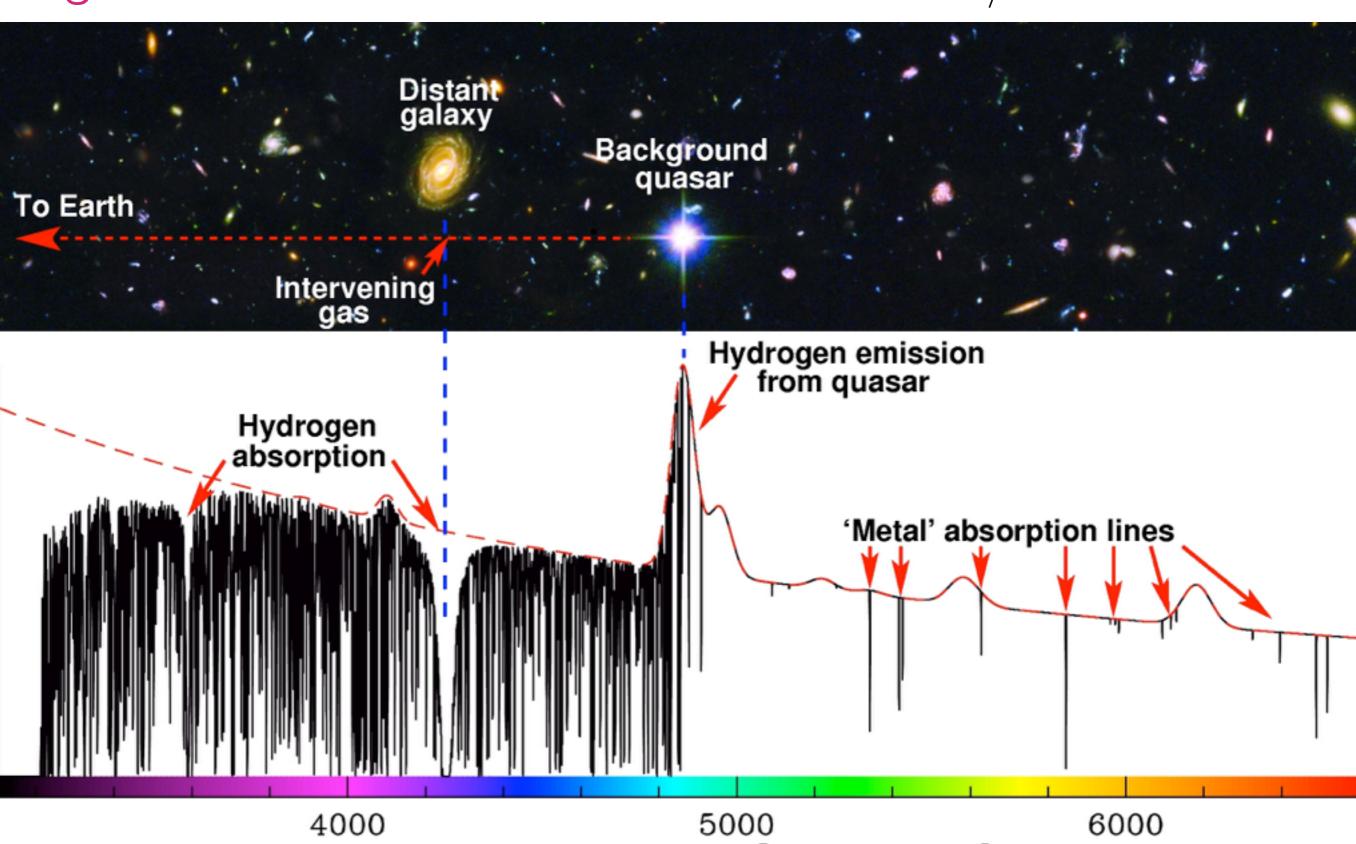
- true primordial detection of Helium in the CMB
- Helium recombines before H, affecting the free electron fraction

=> affects redshift of last scattering and Silk damping tail

CMB only detection of Helium yields 10% level uncertainty (high-l polarization data will yield improvement)



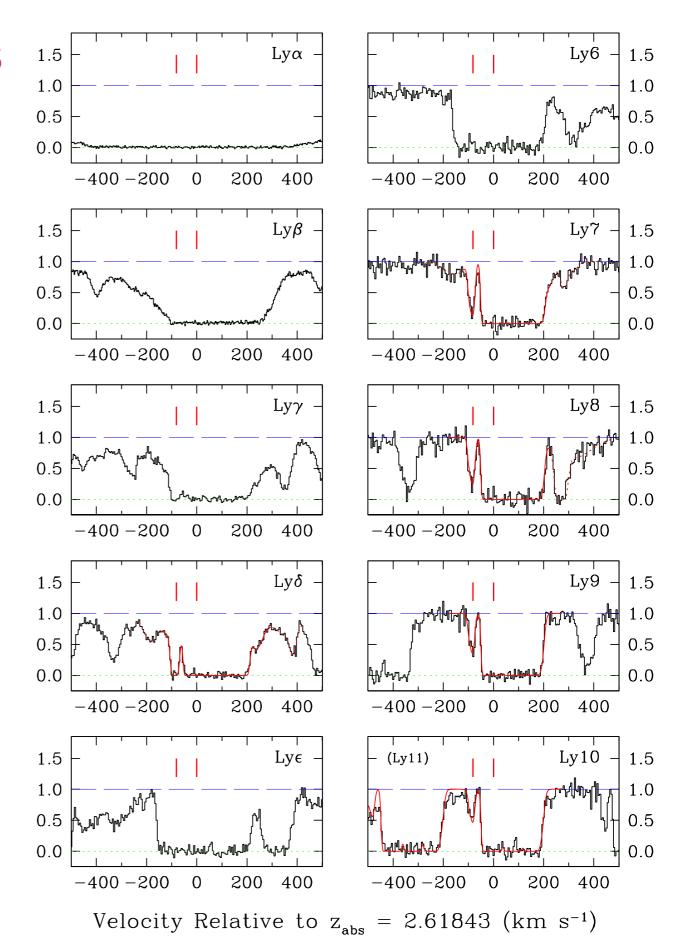
Light element observations Deuterium D/H $\simeq 10^{-5}$



Observed Wavelength [Angstroems]

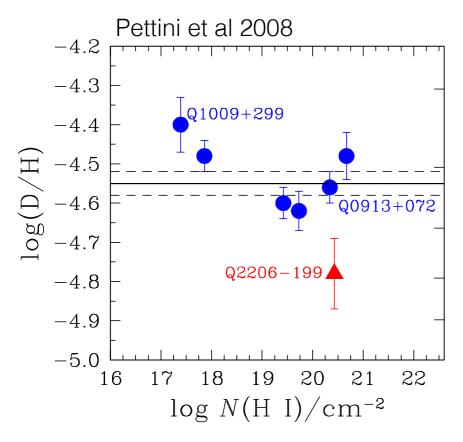
Light element observations Deuterium D/H $\simeq 10^{-5}$

- no known astrophysical sources (monotonic)
- ISM measurements (FUSE) show dispersion in the local gas D-absorption on dust grains?
- high-z QSO systems are the way to go
 - => metal poor Ly-alpha systems have > 98% of primordial D
 - => measured through the isotopic shift from H

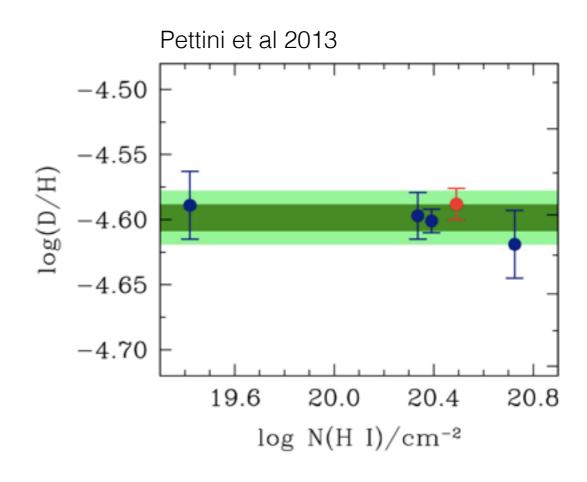


Light element observations

Deuterium D/H $\simeq 10^{-5}$



$$(D/H)_p = (2.81 \pm 0.21) \times 10^{-5}$$



$$(D/H)_p = (2.53 \pm 0.04) \times 10^{-5}$$

=> drastic improvement of the error bar by factor 5 in a few years Now D/H at %-precision!

Lithium observations

- can be observed in atmospheres of stars
- metallicity traces age => stars (formed) at lowest metallicities are thought to represent the chemical composition of the pre-galactic gas he formulas again!

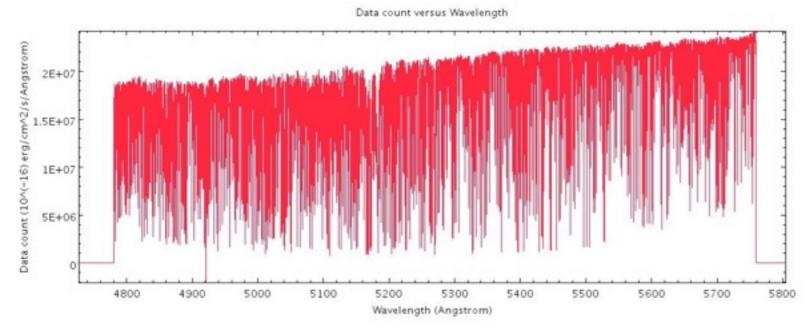
5500

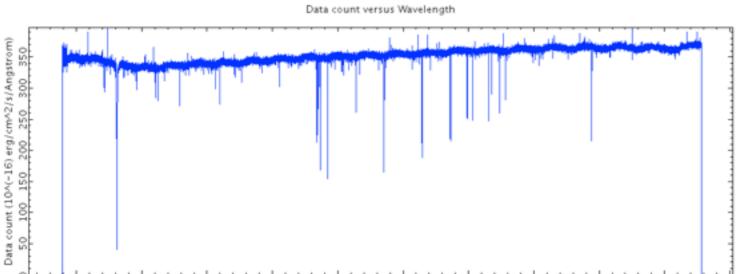
5400

5600

5700

5800





5300

Wavelength (Angstrom)

5200

HD 124897 [Fe/H] = -0.5 light

Spectra obtained with applet "SPLAT" [http://star-www.dur.ac.uk/]

CD-38-245 [Fe/H] = -4

4900

5000

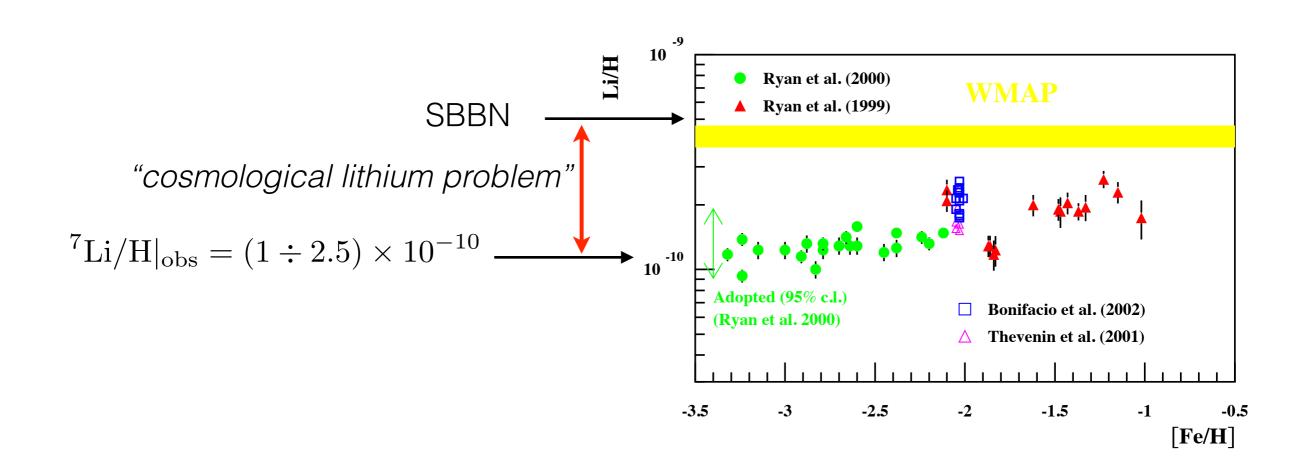
5100

4800

Coc et al 2004

Lithium observations

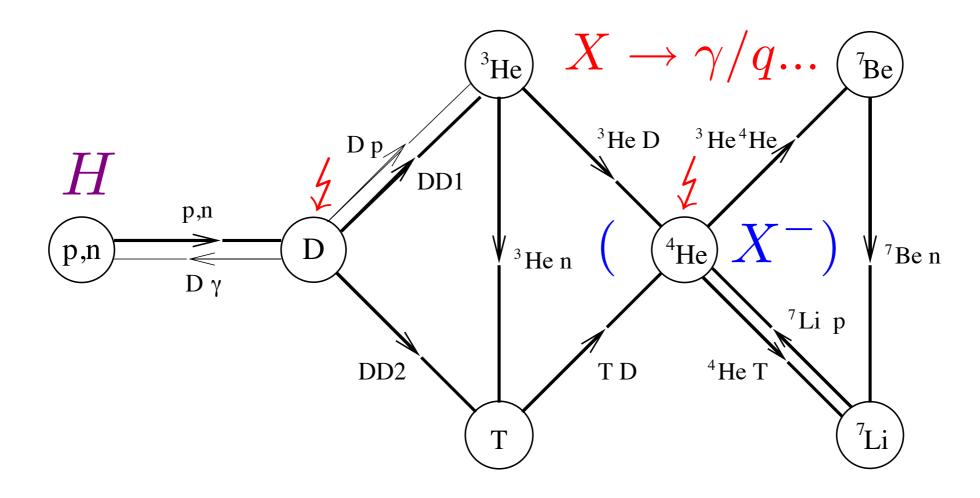
- can be observed in atmospheres of stars
- metallicity traces age => stars (formed) at lowest metallicities are thought to represent the chemical composition of the pre-galactic gas
- Li shows plateau structure with small scatter at lowest metallicities: "Spite plateau" (1982) => points towards primordial origin



SBBN take-home message

- Light element predictions from helium to lithium span roughly 9 orders of magnitude in number
- Impressive agreement with observations of D and He
- One quantitative problem: Lithium abundance is high by a factor of 3-5, with high statistical significance
- Nuclear physics lithium solution is ruled out; solution may be of astrophysical origin but could also signal new physics operative during BBN

Beyond SBBN



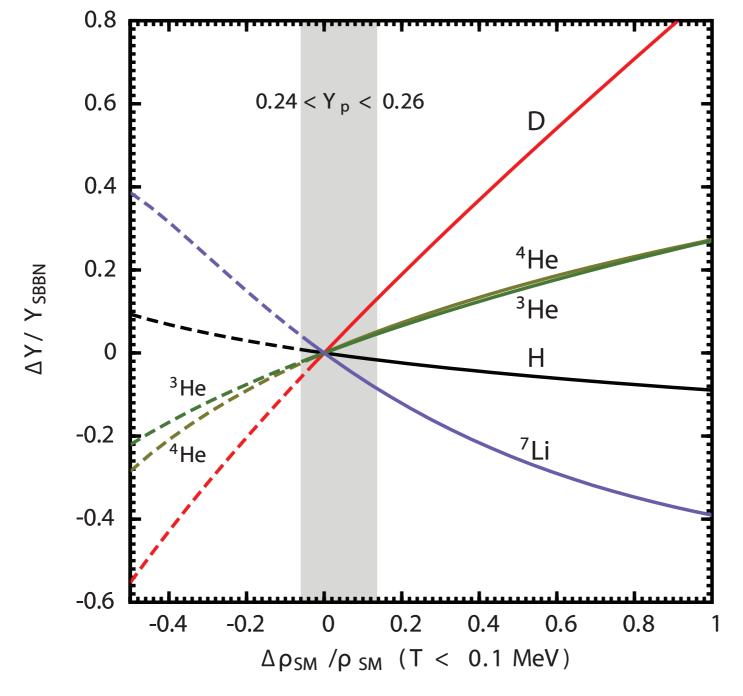
Change in timing

non-equilibrium BBN

catalyzed BBN

Change in timing

$$H_{\rm SBBN} \to H = H_{\rm SBBN} \sqrt{1 + \rho_{dr}/\rho_{\rm SM}}$$





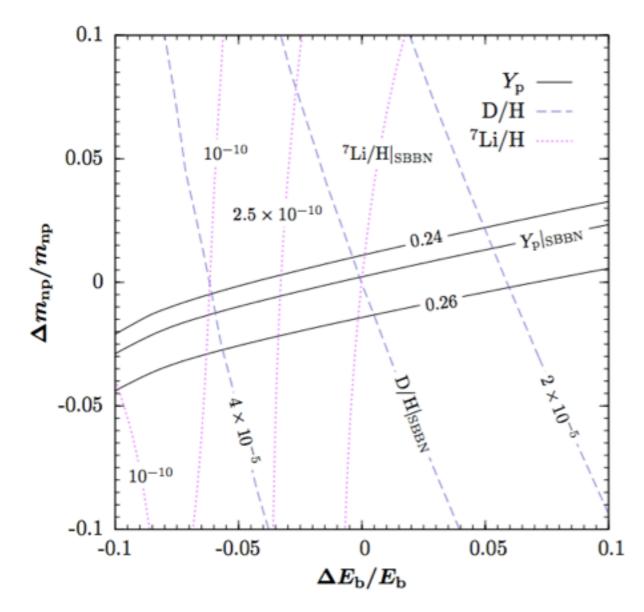
 $N_{\rm eff} = 3.15 \pm 0.23$

Planck 2015

Time evolution of fundamental constants

A time evolution of, e.g. $\frac{\langle \phi \rangle}{M} F_{\mu\nu}^2$ or $\frac{\langle \phi \rangle}{M} m_q \bar{q} q$

- => yields changes in m_q, electric charge, Λ_{QCD} , Higgs vacuum expectation value....
- => induce changes in the reaction rates, nuclear binding, and the position of resonances



BBN: exponential sensitivity on

 Δm_{np} determines n/p freeze out

 E_d determines end of the D-bottleneck

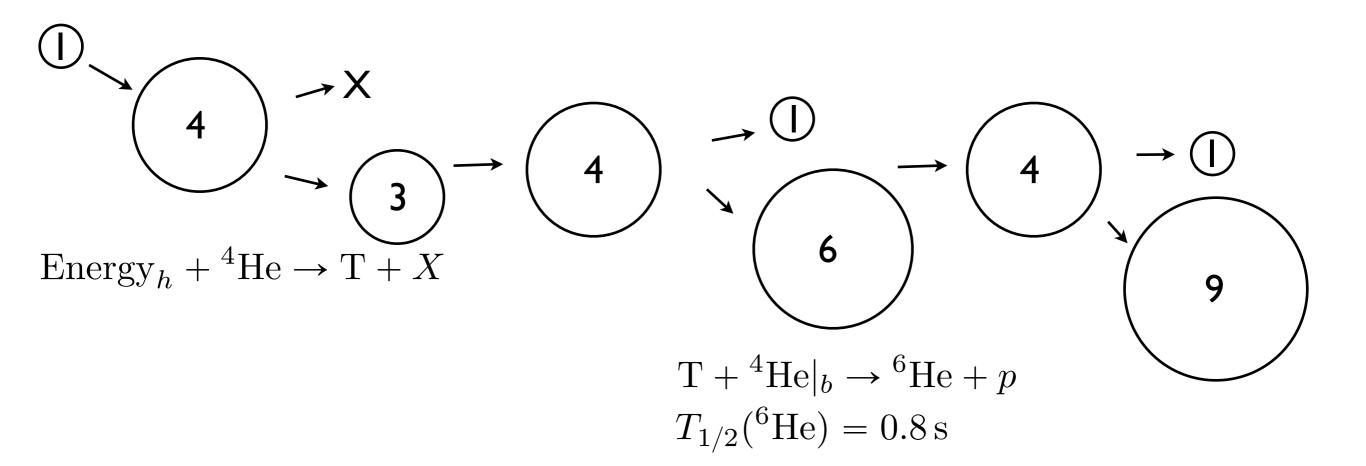
Non-equilibrium BBN Energy injection

- energy release during SBBN (mass conversion into nuclear binding energy)
 - $\sim 2~{\rm MeV/nucleon}~=>$ marginal effect at z = 1 billion
- most prominent class: decays of long-lived particles X
 - => previous works focused on $m_X = \mathcal{O}(100~{\rm GeV})$, e.g. $\widetilde{G} \to SM + \widetilde{\chi}^0$

Dimopoulos 1988;; Kawasaki et al 2004; Jedamzik 2006; Cyburt et al 2009

- => yield electromagnetic and hadronic showers which dissociated light elements
- => drastic departures from the equilibrium picture

non-equilibrium BBN



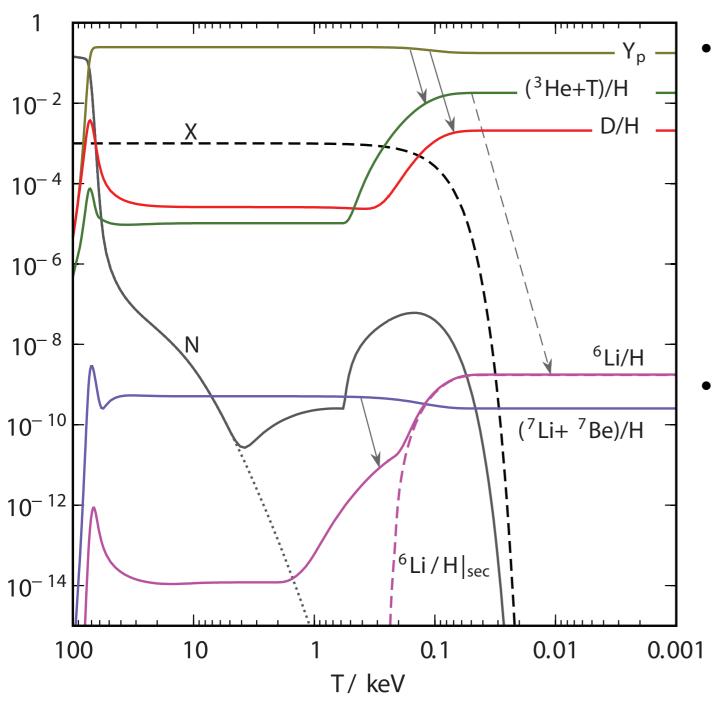
$${}^{6}\text{He} + {}^{4}\text{He}|_{b} \rightarrow {}^{9}\text{Be} + n$$

Pospelov, JP, 2010

Beryllium becomes the BBN "calorimeter"; its abundance is constrained from observations in stars

Non-equilibrium BBN

Electromagnetic energy injection (t > 10^6 sec)



- photons in EM-cascade below e^\pm threshold are not efficiently dissipated
- => spallation of nuclei

Important secondary effect:

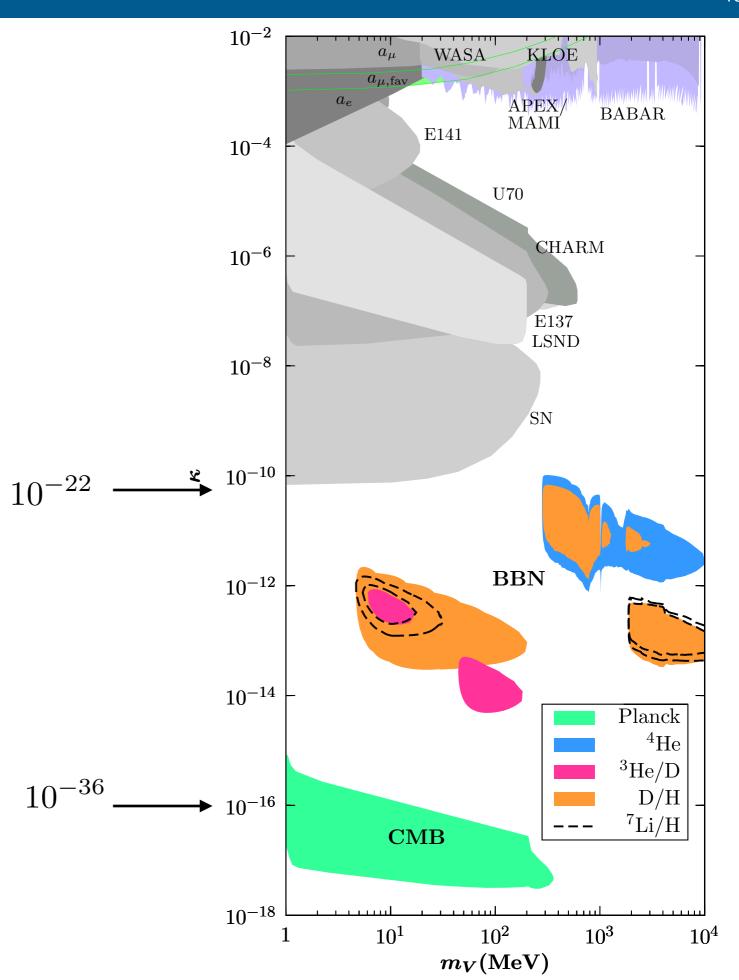
$$^{3}\mathrm{H} + ^{4}\mathrm{He}|_{bg} \rightarrow ^{6}\mathrm{Li} + n$$

$$^{3}\mathrm{He} + ^{4}\mathrm{He}_{bg} \rightarrow ^{6}\mathrm{Li} + p$$

An application to Dark Photons

Cosmology becomes the only test for very feeble couplings to SM

$$\alpha' = (\kappa e)^2/(4\pi)$$



Summary

Lecture III

- Organizational principle of new physics in terms of effective operators in direct detection and at the collider; approach has its limitation, when mediator goes onshell
- With the Higgs discovery, many models fell on July 4, 2012. A minimal extension of the dark sector by a new mediator opens up many new possibilities of phenomenology (e.g. intensity frontier)
- DM may carry a chemical potential (asymmetric DM) => alternative to the WIMP miracle
- Nucleosynthesis is one of the pillars the standard cosmological rests on; its sensitivity to new physics makes BBN a valuable tool to test BSM physics
 => every model of new physics has to pass this cosmological consistency test.

Thank you — and keep up the good work!